

KOLÁŘ IVAN, Masaryk University, Brno, Czechia: CONNECTIONS ON
HIGHER ORDER FRAME BUNDLES AND THEIR GAUGE ANALOGIES

We present two approaches to the torsion of connections on the r -th order frame bundle $P^r M(M, G_m^r)$ of an m -dimensional manifold M . We clarify that the torsion-free connections on $P^r M$ are in bijection with the reductions of $P^{r+1} M$ to the subgroup $G_m^1 \hookrightarrow G_m^{r+1}$. This enables us to introduce the r -th order exponential operator that transforms the classical torsion-free connections on M into torsion-free connections on $P^r M$. Using the methods of the theory of natural bundles and operators, we describe all natural operators transforming the classical torsion-free connections on M into connections on $P^r M$. We outline the generalization of these problems to the gauge-natural prolongations of principal bundles.